An experimental and numerical examination on the thermal inertia of a cylindrical lithium-ion power battery

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Abstract:
Thermal issues are increasingly critical for the scaling-up and integrated deployment of lithium-ion batteries (LIBs). To make battery temperature control more accurate, a concept of thermal inertia was proposed to cylindrical power batteries in the current study. Experimental results showed that the thermal inertia of the battery can greatly affect the thermal behavior during battery discharging process, based on which a battery thermal model was created by COMSOL Multiphysics with infrared imaging technology adopted to experimentally investigate the thermal inertia for a LiFePO4 (LFP) battery. It is evidenced that the model and the corresponding simulation can provide helpful guidance for the thermal behavior control and improve thermal performance. Furthermore, the temperature distribution and variation of the slack period (after discharge) were studied, including internal temperature, surface temperature and temperature difference. Results showed that the battery radius (R) and discharge rate (C) were the major factors that influenced the thermal inertia. In addition, a thermal inertial calculation model was proposed for predicting battery thermal inertia under different operating conditions.

Keywords: Cylindrical lithium-ion power battery; Thermal inertia; Temperature distribution; Infrared imaging

Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Surface area (m²)</td>
</tr>
<tr>
<td>αo, αc</td>
<td>Oxidation/reduction coefficient</td>
</tr>
<tr>
<td>C</td>
<td>Discharge rate</td>
</tr>
<tr>
<td>c</td>
<td>Lithium ion concentration (mol m⁻³)</td>
</tr>
<tr>
<td>cₚ</td>
<td>Specific heat capacity (J kg⁻¹K⁻¹)</td>
</tr>
<tr>
<td>cₑₘₐₓ</td>
<td>Maximum lithium ion concentration (mol m⁻³)</td>
</tr>
<tr>
<td>cₑ</td>
<td>Initial electrolyte concentration (mol cm⁻³)</td>
</tr>
<tr>
<td>D</td>
<td>Diffusion coefficient (m² s⁻¹)</td>
</tr>
<tr>
<td>Eₜₚₑ</td>
<td>Activation energy-electrolyte lithium</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tₛ</td>
<td>The highest temperature at slack period (°C)</td>
</tr>
<tr>
<td>t</td>
<td>Process time (s)</td>
</tr>
<tr>
<td>U</td>
<td>Open-circuit voltage (V)</td>
</tr>
<tr>
<td>V</td>
<td>Voltage (V)</td>
</tr>
<tr>
<td>v</td>
<td>Volume (m³)</td>
</tr>
<tr>
<td>W</td>
<td>Cell with (mm)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Greek letters</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ε</td>
<td>Porosity</td>
</tr>
<tr>
<td>η</td>
<td>Overpotential (V)</td>
</tr>
</tbody>
</table>

* Corresponding author.
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ion diffusion (J mol\(^{-1}\))

\(E_{act}^{i_a}\) Activation energy- exchange current density (J mol\(^{-1}\))

\(E_{act}^{i_s}\) Activation energy- solid phase lithium ion diffusion (J mol\(^{-1}\))

\(F\) Faraday constant (C mol\(^{-1}\))

\(H_a\) Humidity (%)

\(H\) Cell height (mm)

\(h\) Equivalent convection heat transfer coefficient (W m\(^{-2}\) K\(^{-1}\))

\(I\) Current load (A)

\(L\) Thickness (m)

\(Le\) The thickness of the electrode (m)

\(P\) Bruggeman factor

\(Q_t\) Total heat (J)

\(q\) Quantity of heat (J)

\(R\) Radius (m)

\(r\) Resistance (Ω)

\(T\) Temperature (K)

\(T_{amb}\) Ambient temperature (K)

\(T_{sur}\) Surface temperature (K)

\(t_c^0\) Lithium-ion transfer coefficient

\(T_{inc}\) Maximum temperature rise (℃)

\(\Delta T_{max}\) Maximum temperature Difference (℃)

\(T_{ime}\) Maximum thermal inertia (℃)

\(T_h\) The highest temperature (℃)

\(T_l\) The lowest temperature (℃)

\(T_t\) The temperature at discharge termination (℃)

\(\kappa\) Ionic conductivity (S m\(^{-1}\))

\(\lambda\) Thermal conductivity (W m\(^{-1}\) K)

\(\rho\) Density (kg m\(^{-3}\))

\(\sigma\) Electronic conductivity (S m\(^{-1}\))

\(\varphi\) Potential (V)

\(c\) contact resistance heat

\(i\) Ion migration heat

\(o\) ohmic heat

\(ir\) irreversible heat

**Superscripts and Subscripts**

0 Initial value

e Liquid electrolyte

eff Effective values

neg Negative electrode

pos Positive electrode

s Solid phase

re reaction heat

\(r\) Radius direction

\(\varphi\) Circumferential direction

\(z\) Axial direction

**Acronyms**

CC-CV Constant Current-Constant Voltage

EVs Electric Vehicles

IC Internal Combustion

IR Infrared Radiation

LFP LiFePO\(_4\)

LIBs lithium-ion Batteries

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1. **Introduction**

In recent years, electric vehicles (EVs) have become increasingly popular as a solution to problems such as environmental pollution and fossil fuel depletion. EVs use lithium-ion batteries (LIBs) as energy-storage devices because they offer the advantages of stable working voltage, high power and energy density [1]. However, LIBs still suffer from problems such as overheating and large
temperature variance during charging and discharging [2, 3]. Thermal issues are increasingly critical for the scaling-up and integrated deployment of lithium-ion batteries. Such thermal issues in LIBs have limited the development of EVs. Under high current discharge rates, the internal and surface (i.e. external) temperatures of LIBs differ vastly: the former increases rapidly, whereas the latter increases slowly with a certain extent of lag due to the slow heat transfer process, which is called the thermal inertia phenomenon of the battery. When batteries are integrated into parallel or serial connections for a battery pack, their thermal inertia will increase significantly. The thermal inertia of a single cell serves as an important basis for thermal design and thermal management. If the influence of thermal inertia is ignored, batteries may suffer a high potential risk of thermal runaway caused by thermal inertia. Therefore, the knowledge of the thermal inertia behavior is helpful for optimization of battery thermal design.

A large number of studies were conducted to investigate the thermal behavior of batteries to solve their thermal problems and improve associated safety performance. An electrochemical–thermal numerical simulation based on the thermal equilibrium model was an ideal approach to reveal the mechanism underlying the temperature distribution, to evaluate the thermal safety of battery and to refine the thermal design [4-8]. To improve the accuracy of numerical models, previous studies mainly focused on the multi-physical (electrochemical–thermal) models [9-13] when investigating the battery thermal characteristics. These multi-physical models were used to study the distribution and the evolution of the temperature, ion concentration, current density and potential under different experimental conditions. Panchal et al. [14-15] presented a mathematical model to predict the transient temperature and voltage distributions of 18650 cylindrical lithium-ion battery at different discharge rates. Results showed that the increased C-rates could result in increased temperature on the principal surface of the battery. They recently studied the heat flux distributions on a prismatic lithium-ion battery at 1-4C discharge rates under various operating temperatures and boundary conditions [16], and provided significant quantitative data on the thermal behavior of lithium-ion batteries. Wu et al. [17] and Li et al. [18] established different heat effect models, which indicated that under high-temperature conditions, the cycle capacity and the lifespan of LIBs would be significantly deteriorated. Kim et al. [19] developed a thermal model to study the effect of the electrode configuration on the thermal behaviors of a lithium-polymer battery. Their results indicated that the current collecting tabs have a significant impact on the thermal behaviors of the battery. Dong [20] developed a numerical model for predicting the thermal behaviors of the lithium-ion battery. It was indicated that the increase in the temperature rising during the discharging process is higher than that during the charging process. In addition, it was found that the thermal behaviors were closely affected by the entropy change. Niculţa et al. [21] conducted theoretical experimental and numerical studies to investigate the electro-thermal characteristics of lithium iron phosphate (LiFePO₄) battery cells. Results revealed that the central cells in the pack had the highest risk of overheating due to the maximum temperature and the lowest thermal dissipation rate in the central area. Xu et al. [22] studied the temperature distribution and heat generation properties of LIBs and optimized their thermal design through analytical solutions.
Thermal inertia, commonly used for modelling heat transfer, is a material property related to thermal conductivity and volumetric heat capacity, which is a measure of the thermal mass and the heat flux rate which controls the surface temperature of a material. In the research field of heat transfer, a higher value of the thermal inertia means a longer time for the system to reach equilibrium. In fact, thermal inertia is applied in many aspects of engineering and meteorological fields. The thermal inertia of oceans is a major factor influencing climate change [23]. Taking advantage of the thermal inertia of a building to shift the cooling load is an important strategy for commercial buildings [24]. Utilizing the thermal inertia of a district heating network for thermal storage is considered an effective energy-saving method for improving the operational flexibility of combined heat and power [25]. In traditional internal combustion engine-powered vehicles, most cooling pumps are always designed with an off-delay function to overcome the thermal inertia of engine block. The thermal inertia in EV power batteries will have an even stronger impact on the BTMS design and control strategy.

In the current study, the concept of thermal inertia was introduced to cylindrical power batteries for the first time. The thermal inertia of a cylindrical LIB was increasingly critical for their scaling-up and integrated deployment. However, few studies have investigated the thermal inertia as an important basis for the thermal management of battery. The thermal behavior and temperature distribution of a battery are both affected by thermal inertia, which can significantly affect the thermal management. Existing studies on electrochemical thermal models focused on the thermal behavior of batteries during charging and discharging; however, they have not examined the heat conduction process of the slack periods. They either completely ignored or extremely simplified the thermal inertia of a battery pack, and therefore could not predict the accurate temperature change after discharging. Thus, a thermal model for thermal inertia of a cylindrical LIB was created and executed in COMSOL Multiphysics, with both experiments and simulations conducted to analyze the effects of discharge rate C and battery size R on thermal inertia. At the same time, a model for thermal inertia prediction was proposed, providing guidance for further design optimization of a LIB thermal management system.

2. Experimental setup

2.1. Experimental system

Fig. 1 is a schematic diagram of the thermal inertia experiment system. The charge and discharge cycles were regulated by the battery testing system controlled by a built-in programmable software, with current, voltage and resistance data collected. In the current study, the industrial infrared imager was used to measure the thermal performance of the battery cell in the charge/discharge processes, while the T-type thermocouples were used to calibrate the temperature measurement from IR. The measured temperature difference between the infrared imager and the thermocouples has a maximum tolerance of 0.1 °C allowed. It was noted that the ambient light contains infrared ray which may form a reflection on the batteries surface to affect the measurement error of the infrared imager. Therefore, to eliminate such effects, a light shade was applied to block the infrared ray of the ambient light, as shown in Fig. 1 As a result, the maximum measurement error by the infrared imager was less than 0.1 °C. The infrared imager was fixed on a tripod and 0.6 meters from the surface of the battery cell and the lens,
which was perpendicular to the measured surface.

Battery Testing

(a) experimental schematic

(b) experimental setup

Fig. 1. The experiment system.

Table 1. Battery cell parameters

<table>
<thead>
<tr>
<th>Items</th>
<th>Parameters</th>
<th>Items</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell with (W)</td>
<td>18 mm</td>
<td>Weight</td>
<td>42 g</td>
</tr>
<tr>
<td>Cell height (H)</td>
<td>65 mm</td>
<td>Internal resistance</td>
<td>30 mΩ</td>
</tr>
<tr>
<td>Rated capacity</td>
<td>1100 mAh</td>
<td>Max continuous discharge rate</td>
<td>40C</td>
</tr>
<tr>
<td>Rated voltage</td>
<td>3.2 V</td>
<td>Discharge cut-off voltage</td>
<td>2.0 V</td>
</tr>
<tr>
<td>Charge cut-off voltage</td>
<td>3.65 V</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
An LFP 18650 battery was used in the current study, with rated capacity of 1.1 Ah and rated voltage of 3.2 V, as shown in Table 1. The battery was fixed by adiabatic plastic clamps at the edges to ensure that the battery surface was only exposed to air and not touched by any other experimental components.

2.2. Experimental procedures

This study aims to investigate the thermal behavior of the LIB. Therefore, the ambient temperature should be consistent during the experimental process. The ambient temperature was maintained at 25 ± 0.5 °C with a maximum variation of 1 °C. The battery temperature was measured under different charge/discharge rates with a cut-off voltage of 2.00 V. Specifically, the charging process follows the standard CC-CV method, in which a battery was initially charged at a constant current of 0.5 C until the voltage reaches 3.65 V (charge and discharge rates of a battery are governed by C-rates; the capacity of a battery is commonly rated at 1C, meaning that a fully charged battery rated at 1Ah should provide 1A for one hour), and then charged at a constant voltage mode. Then, the charging process was ended when the charging current drops to less than 0.05 C. Table 2 lists the parameters of IR imager, which was well calibrated and applied to measure the battery temperature in both charging and discharging processes. The temperature distribution can be acquired by the infrared imager with high accuracy and resolution since there was no physical contact and the influence of the ambient was eliminated by the shield in the experiment.

Table 2. Infrared imager parameters.

<table>
<thead>
<tr>
<th>Items</th>
<th>Parameter</th>
<th>Items</th>
<th>Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ambient temperature</td>
<td>T&lt;sub&gt;amb&lt;/sub&gt;</td>
<td>Thermal infrared emissivity</td>
<td>0.60</td>
</tr>
<tr>
<td>Ambient humidity</td>
<td>H&lt;sub&gt;a&lt;/sub&gt;</td>
<td>Measuring distance</td>
<td>0.6 meter</td>
</tr>
</tbody>
</table>

Measurement error of infrared imager was restricted by the following aspects: (1) degree of accuracy, T-type thermocouples were calibrated by ice water mixture in a vacuum bottle to ensure the difference between the measured value and the real temperature was no more than 0.1 °C; (2) degree of precision, the measured temperature difference between the infrared imager and the thermocouples was allowed to be no more than 0.1°C during the experiments by adjusting battery surface emissivity; (3) repeatability, at room temperature (25 °C), the surface temperature of the battery was measured several times, the measured temperature difference between the infrared imager and the thermocouples was no more than 0.1 °C; (4) reproducibility, at 50 °C high-temperature test chamber, the surface temperature of the battery was measured several times, the measured temperature difference between the infrared imager and the thermocouples is no more than 0.1 °C.

2.3. Key parameters

The maximum temperature increase (T<sub>inc</sub>) represents the temperature difference between the highest temperature (T<sub>h</sub>) and the ambient temperature (T<sub>amb</sub>) of the battery cell, which is defined and calculated by Eq. (1):

\[ T_{inc} = T_h - T_{amb} \]
The maximum temperature difference ($\Delta T_{\text{max}}$) denotes the temperature difference between $T_h$ and the lowest temperature $T_l$, as shown in Eq. (2),

$$\Delta T_{\text{max}} = T_h - T_l \quad (2)$$

The maximum thermal inertia ($T_{\text{ine}}$) denotes the temperature difference between discharge termination temperature $T_t$ and the highest temperature of the slack period $T_s$, as shown in Eq. (3),

$$T_{\text{ine}} = T_t - T_s \quad (3)$$

### 2.4 Electrochemical thermocouple mode

The 18650 cylindrical LIBs were formed by winding a multilayer of cathode, electrolyte, separator, anode, collectors and other supporting materials. To study its thermal performance during discharging, Fang [26] and Lee [27] simplified the cylinder’s helical structure to a single-layer structure for the convenience of numerical calculations, as shown in Fig. 3. The two-dimensional geometric model of the battery was divided into three areas: nylon axis, active material and stainless-steel shell, with the thickness of each layer being 2 mm, 0.25 mm and 6.75 mm, respectively. The rectangular grid was used for battery mesh model and calculation, a total of 1632 cells were generated in three areas, with the maximum cell size of $6.5 \times 10^{-6}$ m and the minimum cell size of $1.3 \times 10^{-6}$ m. Such a structure assumed that the current density distribution on the electrode was uniform. In fact, during internal particle transfer in the battery, generate/dissipate processes are all completed within a single narrow tunnel. Also, according to this method, the research object will approximately be treated as the single narrow tunnel batteries, in the thickness direction from left to right of single batteries macro physical structure was the anode active material, the separator and the cathode active material, as shown in Fig. 2. The following assumptions were made about the battery: (1) The battery material was evenly distributed and its density was consistent; the quality and volume change of the battery during charging and discharging were ignored. (2) Owing to the minor internal liquidity of the battery, internal convection heat transfer was safely neglected. (3) Radiation dissipation was ignored due to the temperature variation range was limited. (4) The thermal properties of the battery did not change with temperature and SOC.

![Fig. 2 One-dimensional electrochemical model](image-url)
In the process of battery discharge, the positively charged lithium ions are diffused to the surface of Li$_x$C$_6$, which constitute the solid phase of the negative electrode, and electrochemical reactions are carried out to generate a liquid or colloidal electrolyte solution. Lithium-ion diffused through the electrolyte solution to the anode. It moves into the solid phase region through an electrochemical reaction, which contains the particles of positive electrode active material. Due to electronic insulation in the porous diaphragm, forcing the electrons to move according to the circuit or the opposite direction of load. The thermal model was set up according to the principle of electrolyte and solid-phase electrode electron and charge conservation. The control equation and boundary conditions of the battery electrochemical - thermal model are summarised in Table 3.

### Table 3 Control equation and boundary conditions of the battery electrochemical-thermal model [28]

<table>
<thead>
<tr>
<th>Conservation equation</th>
<th>Boundary conditions</th>
</tr>
</thead>
</table>
| **Conservation of charge** | \[
\frac{\partial}{\partial x}\left(\sigma^{ep}\frac{\partial}{\partial x}\phi_s\right) - j_{Li}^{\pm} = 0
\]
| | \[
-\sigma^{ep}\frac{\partial \phi_j}{\partial x}\bigg|_{L=0} = \frac{I}{A}
\]
| | \[
\frac{\partial \phi_j}{\partial x}\bigg|_{L=1} = 0
\]
| | \[
\frac{\partial \phi_j}{\partial x}\bigg|_{L=1,1_s} = 0
\]
| **Electronic conservation** | \[
\frac{\partial}{\partial x}\left(\epsilon_{r}\epsilon_s\frac{\partial}{\partial x}\phi_s\right) + \frac{\partial}{\partial x}\left(\kappa^{ep}\frac{\partial \ln c_s}{\partial x}\right) + j_{Li}^{\pm} = 0
\]
| | \[
\frac{\partial \phi_j}{\partial x}\bigg|_{L=0} = \frac{\partial \phi_j}{\partial x}\bigg|_{L=1,1_s} = 0
\]
| | \[
\frac{\partial \phi_j}{\partial x}\bigg|_{L=1} = \frac{\partial \phi_j}{\partial x}\bigg|_{L=1,1_s} = 0
\]
| **Energy conservation** | \[
\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot \lambda \nabla T + Q_i
\]
| | \[
-\lambda \frac{\partial T}{\partial x}\bigg|_{L=0} = h(T_{amb} - T) \frac{\partial T}{\partial x}\bigg|_{L=1} = 0
\] (LFP)
| | \[
-\lambda \frac{\partial T}{\partial x}\bigg|_{L=0} = -\lambda \frac{\partial T}{\partial x}\bigg|_{L=1} = h(T_{amb} - T)
\] (LFP)
| | \[
Q_i = q_{\nu} + q_{\sigma} + q_{r} + q_{nc} + q_{c}
\]
| | \[
q_{\nu} = j_{Li}^{\pm} (\phi_s - \phi_e - U)
\]
| | \[
q_{\sigma} = \sigma^{ep} \nabla \phi_s \nabla \phi_s + \kappa^{ep} \nabla \phi_e \nabla \phi_e
\]
\[ q_i = \kappa \rho \phi \nabla \ln c_v \nabla \phi, \quad q_{re} = j^{Li} \left( \frac{2U}{cT} \right), \quad q_c = \frac{I^2 R_c}{Av} \]

Q in Table 3 represents all the quantity of heat generation and heat dissipation during the discharge process, including the irreversible electrochemical reaction heat \( q_{re} \), ohmic heat \( q_o \), ion migration heat \( q_i \), irreversible heat \( q_r \) and contact resistance heat \( q_c \). In order to quantify the intensity of electrochemical reaction during high discharge rates of the battery, the Butler-Volmer equation was introduced to calculate the transport current density of the whole battery:

\[
j^{Li} = i_0 \left[ \exp \left( \frac{a_c F}{RT} \eta \right) - \exp \left( \frac{-a_c F}{RT} \eta \right) \right]
\]

where \( i_0 \) is the exchange current density, \( a_c \) and \( a_i \) are transfer coefficients, \( \eta \) denotes the local surface overpotential and \( F \) is the Faraday constant.

The electrochemical-thermal model parameters of the lithium-ion batteries model are shown in Table 4. The parameters of a cylindrical 18650 battery are collected from the literature [29,30] and COMSOL Multiphysics user guide [31].

<table>
<thead>
<tr>
<th>Materials</th>
<th>Cathode</th>
<th>Separator</th>
<th>Anode</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thickness, L (cm)</td>
<td>LiFePO₄</td>
<td>Polyolefin</td>
<td>LiC₆</td>
</tr>
<tr>
<td></td>
<td>142×10⁻⁴</td>
<td>40×10⁻⁴</td>
<td>91×10⁻⁴</td>
</tr>
<tr>
<td>Thermal conductivity, ( \lambda ) (W m⁻¹ K⁻¹)</td>
<td>0.4</td>
<td>0.5</td>
<td>0.4</td>
</tr>
<tr>
<td>Porosity, ( \varepsilon )</td>
<td>0.59</td>
<td>0.42</td>
<td>0.54</td>
</tr>
<tr>
<td>Ionic radius, ( r ) (( \mu ) m)</td>
<td>5</td>
<td>N/A</td>
<td>5</td>
</tr>
<tr>
<td>Maximum lithium ion concentration, ( c_{e,max} ) (mol m⁻³)</td>
<td>31000</td>
<td>N/A</td>
<td>51800</td>
</tr>
<tr>
<td>Initial electrolyte concentration, ( c_e ) (mol cm⁻³)</td>
<td>1.2×10⁻³</td>
<td>1.2×10⁻³</td>
<td>1.2×10⁻³</td>
</tr>
<tr>
<td>Solid phase conductivity, ( \sigma ) (S m⁻¹)</td>
<td>1.0</td>
<td>N/A</td>
<td>0.1</td>
</tr>
<tr>
<td>Solid phase lithium ion diffusion coefficient, ( D_s ) (m² s⁻¹)</td>
<td>2.55×10⁻¹⁰</td>
<td>2.0×10⁻¹⁰</td>
<td></td>
</tr>
<tr>
<td>The diffusion coefficient of lithium ions in electrolytes ( D_e ) (m² s⁻¹)</td>
<td>1.5×10⁻¹⁰</td>
<td>1.5×10⁻¹⁰</td>
<td>1.5×10⁻¹⁰</td>
</tr>
<tr>
<td>Activation energy (electrolyte lithium ion diffusion), ( E_{act}^{D_e} ) (J mol⁻¹)</td>
<td>10000</td>
<td>N/A</td>
<td>10000</td>
</tr>
<tr>
<td>Activation energy (exchange current density), ( E_{act}^{i_0} ) (J mol⁻¹)</td>
<td>30000</td>
<td>N/A</td>
<td>30000</td>
</tr>
<tr>
<td>Activation energy (solid phase lithium ion diffusion), ( E_{act}^{D_s} ) (J mol⁻¹)</td>
<td>50000</td>
<td>N/A</td>
<td>25000</td>
</tr>
</tbody>
</table>
The 18650 lithium-ion battery was composed of a variety of materials and formed with winding structure. The calculation of thermal conductivity in heat transfer was based on the theory of heat resistance, calculating the average thermal conductivity of the battery's radial, circumferential and axial direction respectively, and computation expression as:

\[
\lambda_r = \frac{r}{\sum \frac{\Delta r_i}{\lambda_i}}
\]

(7)

\[
\lambda_{\varphi} = \lambda_z = \frac{\Delta r_i}{r} \sum \frac{\lambda_i}{r}
\]

(8)

\(\lambda_r, \lambda_{\varphi}\) and \(\lambda_z\) are thermal conductivity(W/(m·K)) in the direction of \(r, \varphi\) and \(z\); \(r\) is radius(m) of the battery, \(\Delta r\) is the thickness(m) of each material in radial. \(\lambda_i\) is thermal conductivity(W/(m·K)) of each material in the battery. The thermal conductivity can be obtained by calculation: \(\lambda_r = 1.4556\) W/(m·K), \(\lambda_{\varphi} = \lambda_z = 116.0468\) W/(m·K)

The density of batteries \(\rho\) and the specific heat capacity \(c\) are generally approximated by the weighted average.

\[
\rho = \frac{\sum m_i}{\sum v_i}
\]

(9)

\[
c = \frac{1}{m} \sum c_i m_i
\]

(10)

In the formula, \(m_i, v_i, c_i\) are the mass, volume and specific heat of each component of the battery.

Natural convection heat transfer coefficient \(h = 5\) W/(m·K)

3. Results and discussions

3.1 model verification

In order to verify the reliability of the battery model, the simulation voltage variation curve of 40C discharge was contrasted with the experimental voltage curve. As shown in Fig.4, the simulation results were almost consistent with the experimental results. The maximum error of the electrochemical model was 0.20 V and the average error was 0.12 V. Meanwhile, the reliability of the electrochemical thermo-coupling model can be verified. The simulated surface temperature compared with the experimental temperature, the maximum error was 5.4 °C, the average error was 3.11 °C. The
experimental results of the battery surface temperature shown in Fig.5 were generally consistent with
the simulation results, thus verifying the correctness and reliability of the model. As shown in Table 5,
the error was acceptable, indicating that the model can meet the requirements of subsequent calculation
and analysis.

![Graph showing battery voltage variation](image1)

**Fig.4 Battery voltage variation**

![Graph showing battery surface temperature](image2)

**Fig. 5 Battery surface temperature**

<table>
<thead>
<tr>
<th>Table 5. Model error analysis</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Electrochemical Model</strong></td>
</tr>
<tr>
<td>Maximum error</td>
</tr>
<tr>
<td>Maximum relative error</td>
</tr>
<tr>
<td>Average error</td>
</tr>
<tr>
<td>Average relative error</td>
</tr>
</tbody>
</table>

3.2 The influence of thermal inertia on the surface temperature of the battery

The thermal inertia was mainly caused by the internal heat source and external temperature difference
during the battery discharge process. After the discharge, the internal heat source was no longer in
existence. Due to the presence of internal and external temperature difference, the heat conduction process continued, resulting in a further increase in the surface temperature difference of the battery. Then the battery surface exchanged heat with the surrounding air, and the surface temperature began to drop. In order to simplify the inertia model, two kinds of heat sources were neglected. After the discharge process, there was a certain amount of reaction heat in the process of restoring the equilibrium potential of the battery, this reaction heat was three to five orders of magnitude less than the reversible heat during the battery discharge (depending on the degree of polarization). Therefore, the reaction heat did not play the dominant role in affecting the battery temperature change. When the battery was in high temperature, the internal material began to decompose and produce heat. In this experiment, the battery temperature had not yet reached the temperature threshold of thermal abuse, so there was no side reaction occurred, which was safely ignored.

It was proved that the thermal inertia had a significant influence on the surface temperature of the battery, therefore a reference model was set up for comparison. The basic physical parameters of the control model were consistent with the inertial model. The initial temperature setting was set as follows: the initial temperature was the same as that of the inertia model; the temperature of each layer inside and outside the battery was consistent; the internal and surface were evenly distributed. As shown in Fig. 6, at the end of the 40 C discharge, the temperature change trend in the unsteady uniform heat dissipation model (inertialess) was markedly different from that in the inertia model, with the maximum temperature difference rising to 15.1 °C. As shown in Fig. 7, the increase in discharge rate affected the battery heat generation rate. When the heat generation rate was higher than the heat dissipation rate, then the heat starts to accumulate inside the battery. Under the condition of high discharge rate, due to the high heat production rate and short discharge time, the thermal inertia at 40C discharge can reach 12.1 °C. It was pointed out that thermal inertia exists in the process of battery discharging and had a significant influence on the surface temperature of the battery. In the battery thermal management system, if the influence of thermal inertia was neglected, the temperature prediction of the battery would be significantly far from the true values, thus reducing the thermal management efficiency and causing battery deterioration.
3.3 The influence of battery radius $R$ on thermal inertia

Fig. 8 shows the infrared images of the battery 40C discharge processes under DOD of 20\%, 40\%, 60\%, 80\% and the end of discharge, respectively. According to the experimental infrared imaging results, the axial line analysis of the surface of the battery shows that the temperature distribution of the cell surface was relatively uniform and the temperature gradient was small. As shown in Fig.9, through simulation studies battery slice isotherm distribution showed that the calculating results agreed with the experimental results, the axial temperature distribution of battery was small, and that the radial temperature gradient was larger than axial. Therefore, it can be inferred that the battery characteristic size $R$ would have a great influence on the radial temperature gradient, thus affecting the change of the
thermal inertia. Three models were established by using the 14650, 18650 and 26650 batteries, which were commonly used in commercial cylindrical lithium-ion batteries, with a diameter of 14mm, 18mm and 26mm, respectively. Under the condition that the nylon axis and the thickness of the steel shell were unchanged, experimental results during the 40C discharge showed that the radius size increased with the internal and external temperature difference at the moment of battery discharge termination. As shown in Fig. 10, the 14650, 18650 and 26650 temperature difference between the inside and outside of the battery at the end of the discharge time was 20.4 °C, 23.6 °C and 25.5 °C respectively. It can be inferred that the greater the radius of the coil cylinder, the greater the thermal inertia after the discharge.

![Fig. 8 IR imaging of battery surface temperature.](image1)

![Fig. 9 Isothermal diagram](image2)

![Fig. 10 14650,18650 and 26650 battery temperature distribution at the end of discharge.](image3)

3.4 Thermal inertia calculation model of cylindrical batteries

In order to estimate the thermal inertia of different characteristic sizes and working conditions, the current study presents a model of thermal inertia prediction for cylindrical batteries. The battery surface
temperature rise $T_{\text{inc}}$ ($Y$) was defined as a dependent variable, with independent variables being the discharge rate $C$ ($X_1$), battery radius $R$ ($X_2$) and time $t$ ($X_3$). A multivariate linear regression analysis was performed on the existing data. The data scope was shown in Table 6.

<table>
<thead>
<tr>
<th>Independent variable</th>
<th>Discharge rate $C$ ($X_1$)</th>
<th>Battery radius $R$ ($X_2$)</th>
<th>Time $t$ ($X_3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Range</td>
<td>10-40 $C$</td>
<td>7-13 $mm$</td>
<td>0-120 s</td>
</tr>
</tbody>
</table>

The function form of the data was analyzed as $Y = at^2 + bt + c + dX_1eX_2f$ and the data was brought into the calculation to obtain the parameters of $a$, $b$, $c$, $d$, $e$ and $f$. The parameter values and errors depicted in Table 7.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
<th>Standard error</th>
</tr>
</thead>
<tbody>
<tr>
<td>$a$</td>
<td>$-2.48241 \times 10^{-4}$</td>
<td>$1.40711 \times 10^{-4}$</td>
</tr>
<tr>
<td>$b$</td>
<td>$-0.00995$</td>
<td>$0.01748$</td>
</tr>
<tr>
<td>$c$</td>
<td>$42.4775$</td>
<td>$0.67373$</td>
</tr>
<tr>
<td>$d$</td>
<td>$0.03963$</td>
<td>$0.0131$</td>
</tr>
<tr>
<td>$e$</td>
<td>$2.01517$</td>
<td>$0.08659$</td>
</tr>
<tr>
<td>$f$</td>
<td>$-0.33219$</td>
<td>$0.03572$</td>
</tr>
</tbody>
</table>

The best fitting can be expressed as:

$$Y=-0.000248X_3^2-0.00995X_3+42.4775+0.03963X_1^{2.01517}X_2^{-0.33219}$$

![Graph showing simulation and fitting results of temperature vs. time]
As shown in Fig.11, the fitting result was consistent with the variation trend of the simulation results, and the average relative error was only 4.04%. The accuracy and stability of the thermal inertial calculation model for cylindrical batteries were verified.

4. Conclusion

In the IC engine vehicles, most of cooling pumps were designed with function of off-delay to overcome the thermal inertia of engine block. For the same reason, the thermal inertia in EV battery has a major impact on BTMS design and control strategy. The current study firstly introduced the concept of thermal inertia to cylindrical power batteries, with both the experiment and the simulation indicating that cylindrical LIBs presented evident thermal inertia. Due to the existence of thermal inertia, the LIB temperature increased continuously after discharge and may result in safety problems. In addition, when batteries are used in series and parallel, the thermal inertia increased dramatically. The key effect factors such as battery discharge rate (C) and radius (R) on thermal inertia were investigated through experimental and simulation studies to clarify the thermal inertia of cylindrical LIBs. The model provides an effective basis for describing the thermal characteristics of the battery and for designing a better and accurate thermal management system. An empirical model of cylindrical battery thermal inertia was also proposed, which can be used to estimate the cell surface temperature rise at commonly used range of time, discharge rate and battery radius. Finally, the thermal inertia of cylindrical LIBs under different characteristic sizes and working conditions were summarized:

(1) After a high-rate discharge, a cylindrical LIB showed slower change in surface temperature than in internal temperature, and therefore a large thermal inertia was formed. The maximum temperature difference between the thermal inertia model and the inertialess model was 15.1°C when discharge rate was higher than 40 C. Therefore, thermal inertia cannot be neglected in the thermal design of high-rate LIBs.

(2) For cylindrical batteries, the maximum temperature difference between the inside and outside of the battery showed a significant increase trend with the increase in the discharge rate. Due to the external temperature of the battery increased slowly, the thermal inertia also increased.
At the end of the discharge, temperature distribution inside the battery, and the temperature gradient existed mainly in the radial direction. While the axial and circumferential temperature gradient was negligible. Therefore, with an increase in the battery radius, the radial temperature difference of the battery would increase significantly, thus the temperature falling of battery after-discharge was hindered by the slow outward heat conduction, resulting in an increase in thermal inertia.

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